

§ 5.2 - Present Value

Recall: The compound interest formula

$$\begin{array}{ccc} \text{future} & & \\ \text{value} & \nearrow & \\ & & A = P \left(1 + \frac{r}{m}\right)^{n \cdot m} \\ & \nwarrow & \\ & & \text{present value} \end{array}$$

To find the present value alone, we get

$$\frac{A}{\left(1 + \frac{r}{m}\right)^{n \cdot m}} = P$$

$$A \left(1 + \frac{r}{m}\right)^{-n \cdot m} = P$$

So the present value formula is

$$P = A \left(1 + \frac{r}{m}\right)^{-n \cdot m}$$

Example 1: Find the present value of

(a) 350 BD due in seven years at 5% ^{semi}annually.

$$P = A \left(1 + \frac{r}{m}\right)^{-n \cdot m} = 350 \left(1 + \frac{0.05}{2}\right)^{-2 \cdot 7} = 247.7 \text{ BD}$$

(b) 600 BD due in 5.5 years at 3% quarterly.

$$P = A \left(1 + \frac{r}{m}\right)^{-n \cdot m} = 600 \left(1 + \frac{0.03}{4}\right)^{-4(5.5)} = 509.04 \text{ BD}$$

Exercise 1: Find the present value of

(a) 120 BP due in 2.5 years at 10% compounded weekly.

(b) 200 BP due in 5 years at 5% compounded daily.

(c) 300 BP due in 7 years at 20% compounded

(d) 12000 BP due in one year at 5.3% annually.