

University of Bahrain
Department of Mathematics
MATHS101: Calculus I
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Worksheet: One-sided Limits

Students' Name: _____

1. Consider

$$f(x) = \begin{cases} \frac{x^2 - 4}{x - 2}, & 1.5 < x < 2 \\ 5x^2 + 1, & x \geq 2 \\ \frac{x^2 - 1}{x - 1}, & x \neq 1 \\ 3, & x < 0 \end{cases}$$

Find:

1. $\lim_{x \rightarrow 1^+} f(x)$

2. $\lim_{x \rightarrow 1^-} f(x)$

3. $\lim_{x \rightarrow 1} f(x)$

4. $\lim_{x \rightarrow 2} f(x)$

5. $\lim_{x \rightarrow 0} f(x)$

6. $\lim_{x \rightarrow 1.5} f(x)$

7. $\lim_{x \rightarrow -1} f(x)$

2. Find

$$\lim_{x \rightarrow -2^+} (x + 3) \frac{|x + 2|}{(x + 2)}$$

3. Find

$$\lim_{x \rightarrow 0^+} \frac{x}{\sqrt{x^2}}$$

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