

## University of Bahrain Quality Assurance \& Accreditation Center

| Course Syllabus Form |  |
| :--- | :--- |
| 1. College | Science |
| 2. Department | Mathematics |
| 3. Program | B.Sc. in mathematics |
| 4. Course Code | MATHS 211 |
| 5. Course Title | Linear Algebra |
| 6. Course Credits | 3 |
| 7. Pre-requisites | MATHS 121 or MATHS 101 |
| 8. Course webpage | http://www. abdullaeid.net/teaching/Fall2018/MATHS211.html |
| 9. Course Coordinator | Dr. Abdulla Eid |
| 10. Academic Year | 2018/2019 |
| 11. Semester | First |
| 12. Cour Dere |  |

12. Course Description: Fields, Vector spaces, Linear dependence and independence, Bases, Dimensions, Subspaces, Quotient spaces, Linear transformations, Connection with matrices, Change of bases, Eigen-values, Characteristic polynomial, Minimal polynomial, Canonical forms in simple cases, Real and complex, inner-product spaces, Orthonormal bases, Orthogonal and complex unitary matrices and their eigen-values, Orthogonal and unitary reduction of real symmetric and complex Hermitian matrices.

## 13. Textbook:

- H. Anton, Elementary Linear Algebra, 2013, 11th Edition, Wiley, ISBN-13: 978-1118473504


## 14. References:

1. G. Strang, Introduction to Linear Algebra, 2016, 5th Edition, Wellesley-Cambridge Press, ISBN13: 978-0980232776
2. D. Lay, S. Lay, J. Macdonald, Linear Algebra and Its Applications, 2015, 5th Edition, Pearson, ISBN-13: 978-0321982384
3. D. Cherney, T. Denton, R. Thomas and A. Waldron, Linear Algebra, 2013, online textbook.

## 15. Other Resources:

The instructor's lecture notes and slides that will be given in the class.

## 16. Course Intended Learning Outcomes (CILOs):

Students who successfully complete this course should be able to:

|  | Mapping to PILOs |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CILOs | a | b | c | d | e | f | g | h | i | j | k |
| 1. Manipulate matrix operations, perform row reduction for a matrix and finding the inverse of a matrix. | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |
| 2. Compute the determinant of a square matrix using cofactor expansion and row reduction methods | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |
| 3. Solve systems of linear equations using Gaussian elimination, invertible matrices, and Cramer's rule | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |
| 4. Verify the vector space and subspace axioms | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |
| 5. Prove that a given set of vectors are linearly independent, forms a spanning set or a basis for a given vector space | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |
| 6. Find a basis for the row, column, and null space of a matrix and determine the nullity and rank of the matrix | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |
| 7. Find a transition matrix from an old basis to a new basis | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |
| 8. Find the Eigenvalues and basis for the Eigenspaces for a given matrix | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |
| 9. Determine whether a given matrix is diagonalizable and write its diagonalization | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |
| 10. Verify whether a transformation is a linear or not and find the transformation from the image of a basis vectors | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |
| 11. Compute the kernel, image, rank, and nullity of a linear transformation and explore their properties | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |
| 12. Determine whether a linear transformation is an isomorphism | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |
| 13. Compute the inner product and find the length, angle and distances between vectors | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |
| 14. Find an orthonormal basis of a given vector space using Gram-Schmidt algorithm | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |
| 15. Recognize the properties of special types of matrices such as elementary, hermitian, unitary, and normal matrices | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |
| 16. Apply linear algebra techniques in wide range of real life problems | $\checkmark$ | $\checkmark$ |  |  |  |  |  |  |  |  |  |

## 17. Course Assessment:

| Assessment Type | Number | CILOs | Weight |
| :---: | :---: | :--- | :---: |
| Tests | 2 | Test 1: CILOs 1,2,3,4,5 <br> Test 2: CILOS 5,6,7,8 | $50 \%$ |
| Quizzes/ Homework |  | All CILOs | $10 \%$ |
| Final Exam | 1 | All CILOs | $40 \%$ |


| 18. Assessments Details: |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No | Assessment | Weight | Time | Date | Place | Material |
| 1 | Test 1 | $25 \%$ | TBA | TBA | TBA | TBA |
| 2 | Test 2 | $25 \%$ | TBA | TBA | TBA | TBA |
| 3 | Quizzes / <br> Homework | $25 \%$ | See the homework <br> rules | See the <br> homework rules | See the <br> home- <br> work <br> rules | All Sections |
| 4 | Final Exam | $40 \%$ | $11: 30$ AM -1:30 PM | 13.1 .2019 | TBA | All sections |

## 19. Course Instructor:

| Section(s) | Instructor | Office |
| :---: | :---: | :---: |
| 6 | Dr. Abdulla Eid | S41-2098 |

## 20. Attendance Policy:

Extracts from the University Bulletin regarding withdrawal and enforced withdrawal (Article 31):
A students absence from lectures or classes in excess of $25 \%$ of the total assigned session will result in an automatics withdrawal of the student from the course, regardless of the causes for his/her absence.
(a) A grade of (W) is given to a student who misses $25 \%$ or more of the total sessions assigned to the course if he/she presents a valid excuse for his/her absence.
(b) A grade of (WF) is given to a student who misses $25 \%$ or more, but with no valid excuse.

The classroom environment should be conductive to learning by all. This means, among other things, coming to class on time and prepared. Please no chit-chat talks during the class. Cell phones, graphical calculators and all electronic devices should be turned off and put away during the class and in the exams.

## 21. Academic Plagiarism:

All students are expected to follow the specific rules of academic honesty and plagiarism as per the regulation of professional conduct violations for University of Bahrain students, decision number $4 / 2006$. Please refer the UoB website-Deanship of Students Affairs-Guidance Office.
Cheating is strictly prohibited and will result in serious consequences. In particular, cheating may result in an " F " for the course and be reported to deanship of students affairs. Using of any outside materials, looking at another student's exam or using cell phones might be consider as a cheating (whether or not you get benefit from it). For more information, refer to the student handbook (Article 75).

## 22. Important Dates:

- Sept 16, 2018: First day of the semester (Instruction begins).
- Sept 27, 2018: Last day to drop courses without a 'W' grade.
- Nov 4 - Nov 8, 2018: Mid semester break.
- Dec 6, 2018: Last day to withdraw with a 'W' grade.
- Jan 3, 2019: Last day of instruction.
- Jan 13, 2019: Final exam.

| 23. Weekly Breakdown: |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Week | Date | Topics Covered | CILOs | Teaching Method | Assessment |
| 1 | 16.09.2018 | Matrices and Matrix Operations | 1 | Lecture and problemsolving | Test 1, Final Exam |
| 2 | 23.09.2018 | Inverses, Gaussian Elimination and a method for finding $A^{-1}$ | 1 | Lecture and problemsolving | Test 1, Final Exam |
| 3 | 30.09.2018 | Determinant by cofactor expansion and row reduction Properties of the determinant | 2,3 | Lecture and problemsolving | Test 1, Final Exam |
| 4 | 07.10.2018 | System of Linear Equations | 2,3 | Lecture and problemsolving | Test 1, Final Exam |
| 5 | 14.10.2018 | Real vector spaces and subspaces | 4 | Lecture and problemsolving | Test 1, Final Exam |
| 6 | 21.10.2018 | Linear independence, spanning sets and basis of a vector space | 5 | Lecture and problemsolving | Test 1, Final Exam |
| 7 | 28.10.2018 | Dimension, row space, column space, and null space | 6 | Lecture and problemsolving | Test 1, Final Exam |
| 8 | 04.11.2018 | Rank, nullity, and change of a basis | 6,7 | Lecture and problemsolving | Test 2, Final Exam |
|  | 11.11.2018 | Mid semester break. |  |  |  |
| 9 | 18.11.2018 | Eigenvectors and Eigenvalues | 8 | Lecture and problemsolving | Test 2, Final Exam |
| 10 | 25.11.2018 | Diagonalization General linear transformation | 9 | Lecture and problemsolving | Test 2, Final Exam |
| 11 | 02.12.2018 | General linear transformation | 10,11 | Lecture and problemsolving | Test 2, Final Exam |


| 23. Weekly Breakdown: |  |  |  |  |  |
| :---: | :---: | :--- | :--- | :--- | :--- |
| Week | Date | Topics Covered | CILOs | Teaching <br> Method | Assessment |
| 12 | 09.12 .2018 | Isomorhpisms and matrix for <br> linear transformation | $10,11,12$Lecture and <br> problem- <br> solving | Test 2, Final <br> Exam |  |
| 13 | 16.12 .2018 | General inner product <br> Angle orthogonality | 13 | Lecture and <br> problem- <br> solving | Test 2, Final <br> Exam |
| 14 | 23.12 .2018 | Orthonormal basis and <br> Gram-Schmidt process | 14 | Lecture and <br> problem- <br> solving | Test 2, Final <br> Exam |
| 15 | 30.12 .2018 | Othogonal matrices and quadratic <br> forms | 15 | Lecture and <br> problem- <br> solving | Test 2, Final <br> Exam |
| 16 | 06.01 .2019 | Application of linear algebra | 16 | Lecture and <br> problem- <br> solving | Quiz |

24. Course Weekly Examples and Problems:

| Week | Date | Section | Topics Covered | Problems |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 16.09.2018 | $\begin{aligned} & 1.3 \\ & 1.4 \end{aligned}$ | Matrices and Matrix operations Inverse of a matrix |  |
| 2 | 23.09.2018 | $\begin{aligned} & 1.2 \\ & 1.5 \\ & 2.1 \end{aligned}$ | Gaussian Elimination <br> Finding $A^{-1}$ <br> Determinant |  |
| 3 | 30.09.2018 | $\begin{aligned} & 2.2 \\ & 1.6 \\ & 2.3 \end{aligned}$ | Determinant by row operations solving linear system by using the inverse Cramer's rule |  |
| 4 | 07.10.2018 | 1.1 | Solving linear system by using the Gauss-Jordan elimination, inverse of a matrix, and Cramer's rule |  |
| 5 | 14.10.2018 | $\begin{aligned} & 4.1 \\ & 4.2 \end{aligned}$ | Real vector spaces Subspaces |  |
| 6 | 21.10.2018 | $\begin{aligned} & 4.3 \\ & 4.4 \end{aligned}$ | Linear independence Basis |  |
| 7 | 28.10.2018 | $\begin{aligned} & \hline 4.5 \\ & 4.7 \end{aligned}$ | Dimension row, columns, null spaces |  |
| 8 | 04.11.2018 | $\begin{aligned} & \hline 4.7 \\ & 4.6 \end{aligned}$ | Rank and nullity Change of basis |  |
|  | 11.11.2018 |  | Mid semester break. |  |
| 9 | 18.11.2018 | 5.1 | Eigenvalues and Eigenvectors |  |
| 10 | 25.11.2018 | $\begin{aligned} & 5.2 \\ & 8.1 \end{aligned}$ | Diagonlization Linear Transformation |  |
| 11 | 02.12.2018 | 8.1 | Linear transformation |  |


| 24. Course Weekly Examples and Problems: |  |  |  |  |  |
| :---: | :---: | :--- | :--- | :--- | :---: |
| Week | Date | Section | Topics Covered | Problems |  |
| 12 | 09.12 .2018 | 8.2 | Isomorphisms <br> Matrices for linear transformation |  |  |
| 13 | 16.12 .2018 | 8.4 | 6.1 | Inner product <br> Angle and orthogonality |  |
| 14 | 23.12 .2018 | 6.3 | Othoronormal basis and <br> Gram-Schmidt process |  |  |
| 15 | 30.12 .2018 | 7.1 <br> 7.2 <br> 7.3 | Orthogonal matrices <br> orthogonal diagonalization <br> Quadratic forms |  |  |
| 16 | 06.01 .2019 | Chapter <br> 10 | Selected applications of linear <br> algebra |  |  |


| 25. Grades |  |  |
| :---: | :---: | :---: |
| Letter Grade | Percentage Equivalent | Grade Point Value |
| A | $90-100$ | 4.00 |
| A- | $87-89$ | 3.67 |
| B+ | $84-86$ | 3.33 |
| B | $80-83$ | 3.00 |
| B- | $77-79$ | 2.67 |
| C+ | $74-76$ | 2.33 |
| C | $70-73$ | 2.00 |
| C- | $67-69$ | 1.67 |
| D+ | $64-66$ | 1.33 |
| D | $60-63$ | 1.00 |
| F | Below 60 | 0.00 |

