University of Bahrain
Department of Mathematics
MATHS122: Calculus II
Spring 2016
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## Test 1

Student's Name: $\qquad$ ID: $\qquad$

Section: $\qquad$ Serial Number: $\qquad$

- Do not open the exam until you are instructed to do so.
- Show sufficient work to justify each answer.
- Calculators are allowed but cell phones are not allowed during the exam.
- Exchange of any material such as calculator, pen, eraser is not allowed.
- No questions are allowed.
- You have 1 hour to finish this exam. You can leave only after 30 minutes of the exam.
- There are 3 questions and 5 pages in this exam.

| Question | Points | Score |
| :---: | :---: | :---: |
| 1 | 6 |  |
| 2 | 4 |  |
| 3 | 10 |  |
| Total: | 20 |  |

Question 1 (6 points)
Consider the region enclosed by the curves $y=\sqrt{x}, y=1$, and $x=0$.
(a) Sketch the region above.
(b) Find the volume of the solid generated by revolving the region about the line $x=4$.

Question 2 (4 points)
Find the length of the curve

$$
y=24 x^{\frac{3}{2}}, \quad 0 \leqslant x \leqslant 2
$$

Question 3 (10 points)
(i) Use l'hopital's rule to find the following limits:
(a) $\lim _{x \rightarrow 0} \frac{\sin x-x}{x^{3}}$
(b) $\lim _{x \rightarrow 0^{+}} x(\ln x)^{2}$
(ii) Evaluate the following integrals:
(a) $\int(6 x+5) \cos x d x$
(b) $\int_{1}^{e} 25 x^{4} \ln x d x$

