University of Bahrain Department of Mathematics MATHS122: Calculus II

Spring 2016 Dr. Abdulla Eid



Worksheet 12: Taylor Series

1. Find the Maclaurin series for $f(x) = \tan x$.

2. Find the Taylor series for
$$f(x) = \sin x$$
 at $a = \frac{\pi}{2}$.

3. Find the Maclaurin series for $f(x) = \sin^2 x$. (Hint: Use double angle formula)

4. Find the Macluarin series for the function $f(x) = \sqrt{1+x^2} - \sqrt{1-x^2}$.

- 5. Consider the function $f(x) = \sqrt{1 + x^2}$.
 - 1. Write out the first four terms of the series representation of f(x).

2. What is the maximum error if the first three terms are used to approximate f(x) for $0 < x < \frac{1}{2}$.

6. In many applications, the **error function** is important. It is given by

$$e(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{t^2} dt$$

Find the first four non–zero terms of the error function e(x).