University of Bahrain
Department of Mathematics
MATHS122: Calculus II
Spring 2016
Dr. Abdulla Eid


## Worksheet 12: Taylor Series

Students' Name: $\qquad$

1. Find the Maclaurin series for $f(x)=\tan x$.
2. Find the Taylor series for $f(x)=\sin x$ at $a=\frac{\pi}{2}$.
3. Find the Maclaurin series for $f(x)=\sin ^{2} x$.
(Hint: Use double angle formula)
4. Find the Macluarin series for the function $f(x)=\sqrt{1+x^{2}}-\sqrt{1-x^{2}}$.
5. Consider the function $f(x)=\sqrt{1+x^{2}}$.
6. Write out the first four terms of the series representation of $f(x)$.
7. What is the maximum error if the first three terms are used to approximate $f(x)$ for $0<x<$ $\frac{1}{2}$.
8. In many applications, the error function is important. It is given by

$$
e(x)=\frac{2}{\sqrt{\pi}} \int_{0}^{x} e^{t^{2}} d t
$$

Find the first four non-zero terms of the error function $e(x)$.

