

3. Show that $2\mathbb{Z} \cup 3\mathbb{Z}$ is **not** a subring of \mathbb{Z} .

4. Let R be a commutative ring with unity 1_R . Consider the set

$$S := \{n \cdot 1_R \mid n \in \mathbb{Z}\}$$

Show that S is a subring of R . What is the unity of S ?

5. Show that if $(R, +)$ is cyclic group, then R is a commutative ring.
6. Suppose R is a ring and that $a^2 = a$ for all $a \in R$. Show that R is commutative (such rings are called **Boolean** rings).
(Hint: Show that $-1 = 1$ and find $(a + b)^2$)
7. Show that the centralizer of an element in a ring is a subring.