University of Bahrain Department of Mathematics MATHS122: Calculus II

Spring 2016 Dr. Abdulla Eid



## **Worksheet 7: Polar Coordinates**

Students'	Name:	
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1. Replace the Cartesian equations with equivalent polar equations and vice versa.

1. 
$$y^2 = 4x$$

2. 
$$x^2 + xy + y^2 = 1$$

3. 
$$r^2 \sin(2\theta) = 2$$

4. 
$$r = \csc \theta e^{r \cos \theta}$$

2. Graph each of the following functions in polar coordinates:

1. 
$$r = 2 + 2\cos\theta$$
.

2. "Archimedian Spiral"  $r = \theta$ .

3.  $r = 2 + 2\cos\theta$ .

4. "four-leaved rose"  $r = \sin(2\theta)$ .

5. "Cardioid"  $r = -1 + \cos \theta$ .

6. "fan"  $r = \cos(3\theta)$ .

7. "**Limacon**"  $r = 3 + 2\cos\theta$ .

8. "Limacon with a loop"  $r = 1 - 2\sin\theta$ .

9.  $r = \tan \theta \sec \theta$ . (Hint: What is the corresponding xy equation of this curve?)

10.  $r = \sec \theta$  and  $r = \csc \theta$ .

- 3. Find the area of the following regions:
  - 1. Shaded by the circle r = 2 and the cardioid  $r = 2 2\cos\theta$ .

2. Inside the circle  $r = -2\cos\theta$  and outside the circle r = 1.

3. Find the area of the inner loop of the lima $con r = 2 - 3 \sin \theta$ 

4. 1. Find the length of spiral  $r = \theta^2$ ,  $0 \le \theta \le \sqrt{5}$ .

2. Can anything be said about the relative lengths of the curves  $r=f(\theta)$  and  $r=2f(\theta)$ ,  $\alpha \leqslant \theta \leqslant \beta$ ?